

1. The probability of the symptom A is 25% and the probability of the symptom B (which occurs independently on the symptom A) is 60%. What is the probability that both symptoms are observed in a patient?

- a) less than 25% +
- b) between 50% and 75% -
- c) between 25% and 50% -
- d) more than 75% -

2. A sphere has been enlarged, such that its surface area increased by a factor of 3. Its volume increased by a factor of

- a) 5.2 +
- b) 3 -
- c) 9 -
- d) 1.7 -

3. A curve is described by the equation $x^2 + y^2 + 2x + 4y + 1 = 0$. What is it?

- a) a circle +
- b) a parabola -
- c) an ellipse -
- d) a hyperbola -

4. The function $f(x) = x \cos(x)$ is:

- a) odd +
- b) neither even, nor odd, nor monotonic -
- c) monotonic -
- d) even -

5. What is the distance between points A=[-5,0,3] and B=[0,5,0]?

- a) 7.7 +
- b) 5.3 -
- c) 12.6 -
- d) 3.5 -

6. How many solutions of the equation $|3\pi|x| + 5| = 3$ are there in domain R?

- a) none +
- b) 2 -
- c) 4 -
- d) 1 -

7. Find the center C of a circle given by the equation $x^2 + y^2 - 8x + 6y + 9 = 0$.

- a) C = [4; -3] +
- b) C = [-3; 2] -
- c) C = [2; -4] -
- d) C = [1; 1] -

8. Choose the correct statement for the function $f(x) = (x - 3)(x + 2)$ on the interval [- 5, 2]

- a) $f(x)$ has minimum value at $x = 0.5$ +
- b) $f(x)$ has maximum value at $x = 0$ -

- c) $f(x)$ has minimum value at $x = -5$ -
- d) $f(x)$ has maximum value at $x = 2$ -

9. What is the domain of function $f(x) = \log_2 \left(\frac{5}{|x-5|} \right)$?

- a) all real numbers except 5 +
- b) all positive real numbers except 5 -
- c) all positive real numbers -
- d) all real numbers -

10. What is the range of function (the set of all value of the function) $f(x) = 4 \cos \left(\frac{\alpha}{4} \right)$

- a) $\langle -4; 4 \rangle +$
- b) $\left\langle -\frac{1}{4}; \frac{1}{4} \right\rangle -$
- c) $\langle -1; 1 \rangle -$
- d) $(-\infty; \infty) -$

11. How many combinations of 5 different alphanumeric characters (repetition is not allowed) are there? Alphanumeric is a combination of alphabetic (26, case insensitive) and numeric characters.

- a) 376,992 +
- b) approx. 60.5 millions -
- c) approx. 45.2 millions -
- d) 658,008 -

12. What is the sum of the 1st and 6th term of an arithmetical sequence if the sum of first 6 terms of this arithmetical sequence is 30?

- a) 10 +
- b) 12 -
- c) 6 -
- d) 5 -

13. There are 6 black and 4 white balls in a bowl. What is the probability P that at least one of two randomly picked balls is white?

- a) $50\% \leq P < 100\%$ +
- b) 100%, at least one of picked balls must be white -
- c) $0\% < P < 50\%$ -
- d) 0%, both balls must be black -

14. What is the 1st term of a geometric sequence if the 3rd term is 5 and 5th term is 25?

- a) 1 +
- b) -15 -
- c) -5 -
- d) $\sqrt{5}$ -

15. Simplify the expression: $\frac{a^{-3}b^3}{\sqrt{a^{-4}b^6}} \log_a a^4$

- a) $\frac{4}{a}$ +
- b) $\frac{b}{a} - 4$ -
- c) ab^{-3} -
- d) $a+4+b$ -

16. Choose the smallest integer constant b so that the quadratic equation $3x^2 + bx + 1 = 0$ has two real solutions:

- a) 4 +
- b) 1 -
- c) 2 -
- d) 3 -

17. What is the solution of the inequality $\frac{2|x-3|}{3} > 4$

- a) $(-\infty, -3) \cup (9, \infty)$ +
- b) $(-\infty, -3) \cup (3, \infty)$ -
- c) All real numbers except -3 a 3 -
- d) $(-3, 3)$ -

18. What is the length of leg (cathetus) of an isosceles right-angled triangle (i.e. both legs - catheti - are equal) whose area is 25?

- a) $5\sqrt{2}$ +
- b) $2\sqrt{5}$ -
- c) 10 -
- d) $\sqrt{10}$ -

19. Which of the following vectors is perpendicular to the vector $\mathbf{u}=(2, 3)$

- a) $(-3, 2)$ +
- b) $(2, 0)$ -
- c) $(3, 0)$ -
- d) $(3, 2)$ -

20. If $\pi < \alpha < 2\pi$ and $\sin(\alpha) = -0.37$ what is the value of $\sin(\alpha - \pi)$?

- a) 0.37 +
- b) $\cos \alpha$ -
- c) $-\cos \alpha$ -
- d) -0.37 -

21) The original statue is 1.5 m high. An enlarged copy of that statue is 3 m high. What is the ratio of the volume of the original statue to the volume of its enlarged copy?

- a) 1:8 +
- b) 1:4 -
- c) 1:2 -
- d) 2:3 -

22. Volume of a cone is given by the formula:

- a) $\frac{1}{3} \pi h r^2 +$
- b) $\pi h r^2 -$
- c) $\pi h r -$
- d) $\frac{1}{2} h r^2 -$

23. Let C be a circle circumscribing a square S. Then the area ratio C/S of the circumscribed circle C and the square S is:

- a) $\pi/2 +$
- b) $3/2 -$
- c) $\sqrt{2}/2 -$
- d) $\pi -$

24. What is the total surface area of a sphere if its volume is 10π ?

- a) $15.3\pi +$
- b) 12 -
- c) $2.5/\pi -$
- d) $10/\pi -$

25. Let i is the imaginary unit defined as $i^2 = -1$. Simplify the expression of $-1+i^{11}$

- a) $-1-i +$
- b) 0 -
- c) $-1 -$
- d) $-1+i -$

26. What is the volume of the cylinder with a radius of 3 and a height of 7?

- a) $63\pi +$
- b) 21 -
- c) 441 -
- d) $42\pi -$

27. What is the sum of all even numbers from 20 to 100 ?

- a) 2460 +
- b) 4000 -
- c) 2400 -
- d) 4800 -

28. What is the solution of the inequality $\log_{10}(1-4x) \geq 0$?

- a) $(-\infty; 0) +$
- b) $(-1; 4) -$

c) $(-\infty; \infty)$ -

d) $\left(0; \frac{1}{4}\right)$ -

29. Each interior angle in a regular hexagon is

a) 120° +

b) 60° -

c) 108° -

d) 136° -

30. What is the smallest period of the function $f(x) = 2 \sin(3x)$?

a) $\frac{2\pi}{3}$ +

b) $\frac{3\pi}{2}$ -

c) π -

d) $\frac{3}{2}$ -